

Design and test of a 300Wh composites flywheel energy storage prototype with active magnetic bearings

Xingjian DAI, Kai ZHANG and Xiao-zhang ZHANG

Department of Engineering Physics
Tsinghua University
Beijing, 100084 (P. R. China)

Phone/Fax number: +0086 10 62784518/+0086 10 62782658, e-mail: daixj@mail.tsinghua.edu.cn

Abstract. A flywheel energy storage prototype was designed and built to get high energy density and low bearing loss. The aluminium alloy hub formed by thin plate and shell connected the bearing shaft and the rim which was composed by glass fibre and carbon fibre reinforced composite. Finite element analysis on stress field of the composite flywheel indicated that the flywheel could run at the rated speed of 700 r/s (rotation per second) safely. The flywheel was supported by 5-degrees of freedom active magnetic bearings (AMBs). The flexible modes of the rim-hub-shaft system were analyzed by using finite element (FE) based software. The complex non-synchronous vibration was observed, analyzed and suppressed during testing of the flywheel system.

The control method of adding phase compensator to the velocity channel in the cross feedback controller was presented to make the supporting AMBs work better while the flywheel passed through its first flexible mode. The field balancing at high speeds enabled the flywheel to reach the speed of 475 r/s with small amplitude of synchronous response.

Key words

Flywheel energy storage; Composites; Active magnetic bearings

1. Introduction

Application of high speed flywheels as mechanical batteries to store energy becomes increasingly attractive in recent years [1]. In opposition to chemical batteries, the life of AMB flywheels has no degradation during the entire design life. A spinning flywheel has capability to accumulate a large amount of kinetic energy. Therefore, having an integrated motor/generator, the well controlled flywheel can be used not only for the attitude control but also for energy storage in spacecraft [2,3].

One of the main sources of energy loss in flywheels is attributed to bearings. With the introduction of frictionless active magnetic bearings, the efficiency of flywheels for energy storage has been increased to an economically useful level. Electrical active magnetic bearings (AMBs) satisfy the frictionless condition but require advanced control systems [4, 5]. Although the super-conducting bearings have been developed to replace conventional bearings [6, 7], they require cryogenic conditions, and AMBs still remain the best bearing alternative for flywheels in spacecraft application.

To demonstrate the possible space application of the advanced composite flywheel with AMBs, the experimental high speed (in rated rotational frequency of 700Hz) FES-AMB system was designed and built in Tsinghua University. The stress and strain field of the flywheel was solved by FEM, which indicated that the structural failure would not happen while the rotational speed being up to 700 r/s. It was found difficult to use the conventional cross feed back control to make the flywheel stable when it passes through the resonant vibration district because of the flexible mode due to the flexible hub connection between the shaft and the rim. Compared with the past literature, the new challenge is the coupling between the strong gyroscopic and the flexible mode resonance at the high speed around 400 r/s.

The complex nonsynchronous vibration behaviour was observed and analyzed during experimental testing of the flywheel system with flexible components. Several control methods were successfully applied to suppress the unexpected modal vibrations. The AMB controller was revised and substantially improved to guarantee stable operation when the flywheel passed two rigid modes and the first flexible mode.

2. Flywheel Structural Analysis

A. Flywheel AMBs System

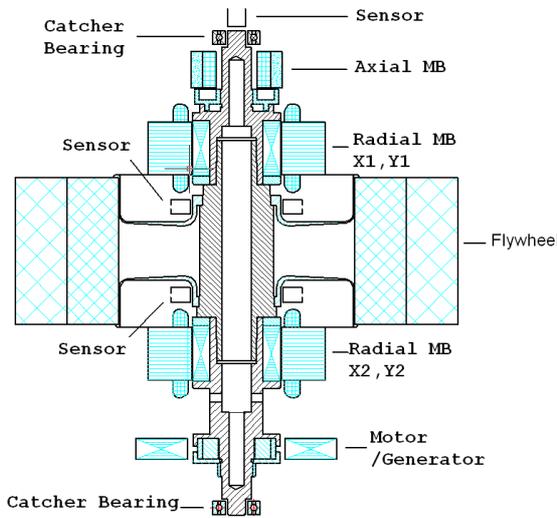


Fig. 1 Flywheel AMBs system

The flywheel levitated by magnetic forces in five degrees of freedom is shown in Fig. 1. The composite rim is connected to the shaft through the aluminum hub. The radial and axial magnetic forces act on the shaft to levitate the flywheel. The flywheel AMBs system has two rotordynamic characteristics. One is the strong gyroscopic effect due to high speed and the large polar moment of inertia, and the other one is the flexible modes in frequency lower than the rated rotational frequency of 700 Hz, which is due to the fact that the flywheel has hub with low rigidity.

Table 1 Parameters of the flywheel

Mass	11.9 kg
Diameter	300 mm
Length	100 mm
Polar momean of inertia	0.13 kgm ²
Diameter moment of inertia	0.087 kgm ²
Rate speed	700 r/s
Sotred enery	340 Wh

B. Rim-hub Stress Analysis

One of main concern of flywheel technology is how to improve the flywheel rotating speed due to the energy stored being proportional to the square of the speed. The specific energy is proportional to the specific strength of materials. Therefore, the fiber-reinforced polymer composites with high specific strength are usually used as the rim materials [8]. The composite rim is attached to a metal shaft through a metallic web or spoke hub which compensates the deformation difference between the rim and the shaft under the high speed running condition. The design procedure was discussed in reference [9].

In the detail design, the finite element analysis is employed to know the stress and strain field of the flywheel composition. The composite rim is either press-fit or

shrink-fit to the metal hub due to the deformation of the rim is much greater than the hub under centrifugal load. In our test flywheel case, the shrink-fit size is 0.30 mm. The composites rim is composed by two rings by winding fabrication method. The inner ring is glass fiber reinforced polymer (GFRP) and the outer ring is carbon fiber reinforced polymer (CFRP).

Table 2 Mechanics parameters of flywheel materials[9]

	E_x	E_z	ρ	σ_{LS}	σ_{TS}	σ_b
	GPa	MPa	kg·m ⁻³	MPa	MPa	MPa
GFRP	15	65	2100	1600	30	-
CFRP	7	130	1550	1800	20	-
7050	72.5	72.5	2800	-	-	570

The plane axial-symmetrical model was used to calculate the stress of flywheel under rotation centrifugal load in FEM analysis. In the elastic calculation, the first load step is shrink-fit size being 0.3 mm, the second load step is centrifugal load under the rotational speed of 700 r/s. The highest Von Mises stress of the aluminum alloy hubs is 330 MPa, being lower than the stress limit of aluminum alloy 7050. The maximum stress value of the composites rim was shown in Table 3. The rim materials are safe while the maximum stress failure criterion could be applied.

Table 3 The maximum stress in rim

Composite	σ_r /MPa	σ_θ /MPa	σ_z /MPa	σ_{LS} /MPa	σ_{TS} /MPa
GFRP	19.4	470	6.9	1700	30
CFRP	13.1	617	4.1	2300	20

Fig. 2 displayed the radial displacement of hub. The hub will expand 0.31 mm in radial direction. Fig. 3 indicated that there are enough press force between the hub and the rim, which make sure the two parts keeping in fixed contact.

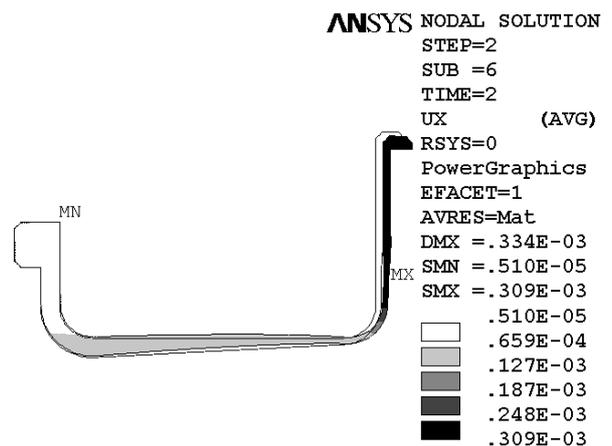


Fig. 3 Deformation of hub (m, 700 r/s)

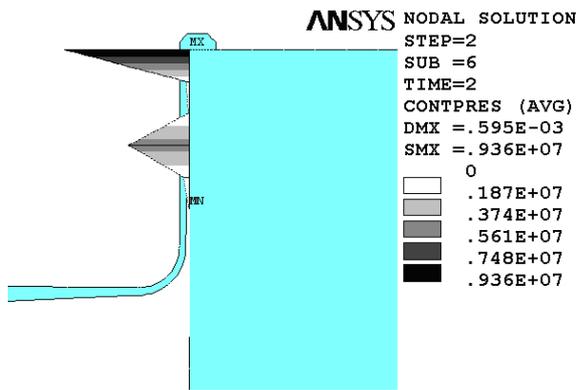


Fig. 3 Rim-hub contact pressure (Pa, 700 r/s)

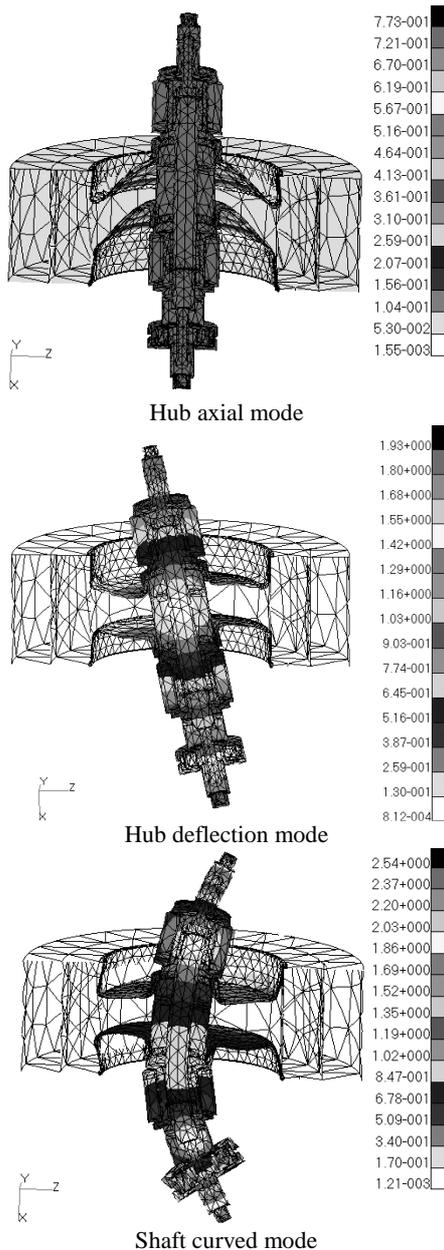


Fig.4 Flexible hub-rim-shaft modes

3. Modal Vibration Analysis

A. Calculation

In the simplified modal vibration analysis of flywheel-bearing system, the flywheel could be considered as a rigid disk locating at the middle of a rigid shaft supported on active magnetic bearings. The performance of the precession in lower frequency and the nutation in high frequency split a lot with the growing rotating frequency due to gyroscopic effect of the flywheel in thin disk form. The splitting modes make the system be parameter-dependent and pose a problem for the AMB controller. The splitting modes will behave as the sub-harmonic and super-harmonic vibration when the modal damping become decaying as the flywheel speed growing up.

The hub with good ability of deformation has the function of connection between the composite rim and the metal core shaft. However, the stiffness of the thin shell is not high enough to make the flexible modal frequency of the rim-hub-shaft system being bigger than the rated rotational frequency (700 Hz).

For such a system composed by rim, shell hub, metal core shaft and bearings, the finite element methods can be quite useful to obtain its vibration mode parameters. In this research ANSYS package has been employed to reveal the flexible modes of the flywheel in its non-rotating state. The analysis indicated that there were three flexible modes with frequency under 1000Hz. The first is a “hub axial” mode, when the hub deforms mainly in axial direction (see Fig. 4), with the frequency of 225.8 Hz. The second is the “hub deflection” mode, as shown in Fig. 4, at the frequency 332.4Hz. The last modal frequency is 937.5Hz, where the modal shape is expressed as the bending of the core shaft. (see Fig. 4).

B. Identification of Modal Frequency

Both the impact test and the force excitation via AMB were used to extract natural frequencies. In the impact test, the impact force was acted on the flywheel-shaft in freely suspended state along both the radial and axial direction separately by the hamper. The sine sweep force excitation test is convenient and useful to obtain the vibration performance of the AMB supported rotors because the excitation and the response can be easily measured.

Table 2 Comparison of the modal frequency / Hz

Mode	Hub axial	Hub deflection	Core shaft bending
Calculated results	225.8	328.4	917.3
Impact test	210	320.0	900
Electric-magnetic excitation	---	340.0	940

To arrive at the speed of 700rps, the flywheel has to pass through the three resonance speeds, two rigid (i.e., cylindrical and conical) and the flexible hub deflection. The hub axial mode was not considered because there is no obvious excitation along the axial direction. The first flexible modal frequency (328Hz) of the hub increases greatly because of strong flywheel gyroscopic effects.

The possible three kinds of nonsynchronous modal vibrations may occur during the start-up process.

4. Nonsynchronous Vibrations

A. Levitation at Zero Speed

The very basic requirement for AMB rotor systems is to achieve stable levitation, where the shaft remains in concentric position at the bearings.

The high order modal vibration was found in the static levitation, which could be attenuated by adding damping in the controller. The frequency of 350 Hz is attributed to hub deflection mode, which can be lowered by the loop shaping technique which means to add additional filter into the controller to change the phase and gain characters at a local frequency range. The third frequency of 950Hz in peak response value belonged to the first flexible shaft mode, which can be damped by adding a notch filter in the controller. The improved PID controller at zero speed made the maximum vibration amplitude being lower than 1 μm .

B. Subharmonic Vibration

After the stable levitation at zero speed is achieved, the flywheel dynamics should be tested during the speeding up. Complex vibration phenomenon was observed during this process. Figure 5 presents large subharmonic vibration measured at the running speed of 82 r/s. The center of the flywheel follows an unstable trajectory. Spectrum analysis indicates that this is the natural backward precession in low frequency of 8 Hz. The subharmonic vibration amplitude may inflate and make the shaft to contact the backup bearings.

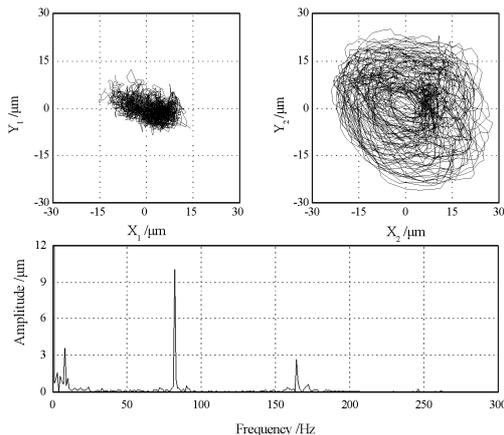


Fig. 5 The precession in low frequency

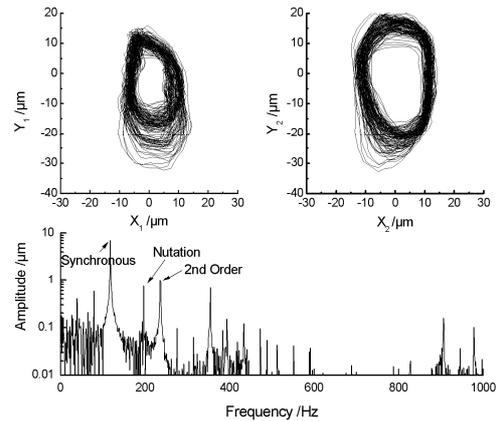


Fig. 6 The nutation in high frequency

C. Superharmonic Vibration

The running of flywheel with strong gyroscopic effect caused instability in the flywheel-hub-shaft bearings system. The PID controller could not confirm the stable running of the flywheel in speeding up. The cross feedback control techniques were presented to lead better system performance [10].

Under the positive displacement cross feedback control, the flywheel has been run to 119 r/s without subharmonic vibration. However, the superharmonic vibration occurred at this time. The spectrum components seem to be very complex. Fig.6 indicates that the superharmonic motion is mainly composed by the 2nd order vibration and the nutation. The nutation could be suppressed by the minus cross feedback in the displacement channel and the minus cross feedback in the velocity channel. On the other hand, the positive displacement cross feedback would suppress the precession but excite the nutation. Therefore, the displacement cross feedback factor must be select carefully. Considering the precession frequency being very low and the nutation frequency being very high, it will get better results to add a low-pass filter into the positive displacement cross feedback channel and add a high-pass filter into the minus displacement cross feedback channel [11].

The elaborate combined application of the low-pass or high-pass filter and the positive or minus displacement cross feedback produced good result which exhibited as the smooth operation of the flywheel up to 280rps.

D. Flexible Modal Vibration

Both the subharmonic precession and the super-harmonic nutation discussed above were rigid modes of the flywheel-bearing system. The flywheel keeps rigid body state. The other kind of super-harmonic vibration can be the flexible shell mode vibration. Fig. 7 shows the observed 3 times harmonic vibration whose frequency is attributed to the flexible hub radial mode. The excitation source was from the bearings' electromagnetic forces with components in high frequency. In the application of "loop shaping" method as mentioned above, the adjusting parameters were selected to get better mode damping of

the flexible rub radial mode. The flywheel was running up to 170 r/s without the flexible modal vibration.

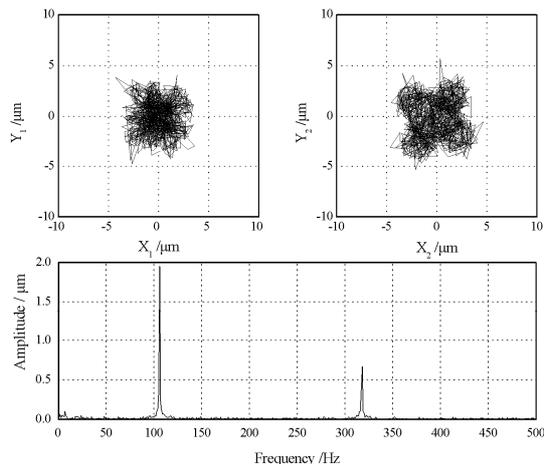


Fig. 7 The flexible modal vibration at low speed

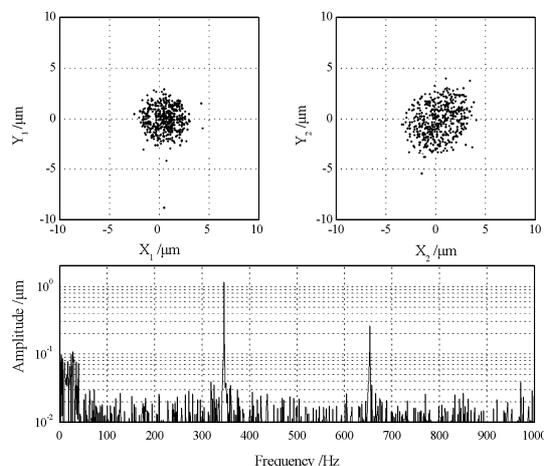


Fig. 8 The flexible modal vibration at high speed

5. Passing through the Flexible Critical Speed

The dynamics analysis indicated that the flywheel-ABMs system should pass through the flexible critical speed as high as 400 r/s. The nutation was observed again as the flywheel run to 346 r/s (see Fig. 8). To suppress the nutation near the flexible modal resonance, the “phase compensator” was added to the velocity cross feedback channel of the controller. The phase compensator alters the gain-frequency and phase-frequency characters of the velocity cross feedback channel and provides additional phase lead for the controller. Then, the flywheel ran to 360 r/s smoothly.

Although AMBs have the ability to compensate the unbalance of the rotor, the unbalance compensation scheme was not used because the concern was focused on the suppression of the nonsynchronous vibration. The flywheel-AMB system was balanced in the field. The two-plane-effect-coefficient balancing method was employed to achieve smooth speeding up with residual unbalance response (seeing Fig. 9). Several balancing experiments were conducted at speeds 130, 166, 257 and 300r/s.

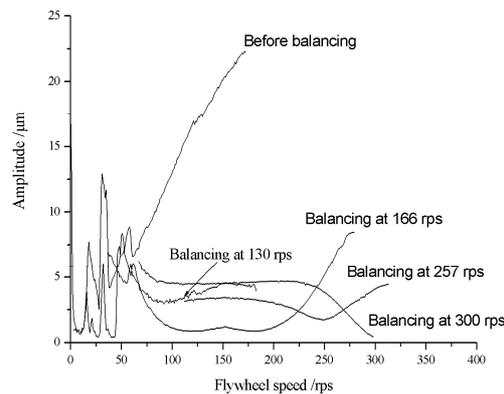


Fig. 9 Balancing at different speeds

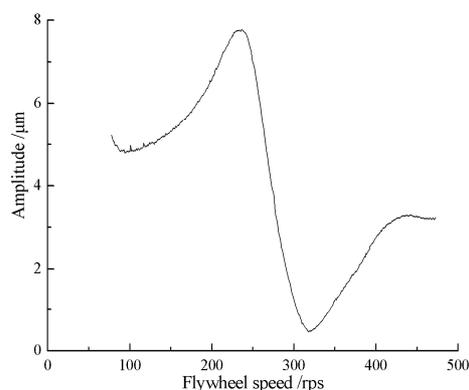


Fig. 10 The unbalance response in high speed running

After numerous trials with the controller, and careful balancing, the flywheel was able to pass the critical speed of 420 r/s and run up to the speed of 475 r/s, as shown in Fig. 10. The AMB flywheel was not run at higher speeds because that the temperature became very high due to both the wind loss in the chamber without high vacuum and the heating from the eddy current loss of the magnetic bearings. The improvement of the vacuum condition and the lower power control of AMBs should be studied further to enable the flywheel run to the rated speed of 700 r/s in the future.

6. Conclusion

The structural stress analysis indicated that the material failure would not happen when the flywheel was speeded up to 700 r/s. The modal analysis of the AMB flywheel system indicated that both the rigid modes and the flexible modes were presented in the system. The flexible mode manifested as the hub deflection shape because of the application of the thin aluminium shell with low stiffness. The prediction was similar to the test results. Several control methods such as the loop shaping, the notch filter, and the cross feedback were combined to control the nonsynchronous vibrations of the flywheel-AMBs system. The new control method of adding phase compensator to the velocity cross feedback channel was presented and it made AMBs performing well while the flywheel passes the high critical speed at the first flexible

mode. The in-field balancing at high speeds made the flywheel run to the speed of 475 r/s with small synchronous response.

References

- [1] P. J. Hall, E. J. Bain, "Energy-storage technologies and electricity generation", *Energy Policy*, 2008, Vol. 36, pp. 4352-4355.
- [2] Renuganth Varatharajoo, "A combined energy and attitude control system for small satellites", *Acta Astronautica* 2004, Vol. 54, pp. 701-712.
- [3] B. H. Kenny, "Control of a high-speed flywheel system for energy storage in space applications", *IEEE transactions on industry applications*, 2005, Vol. 41(4), pp. 1029-1038.
- [4] C.R. Knospe, "Active magnetic bearings for machining applications", *Control Engineering Practice*, 2007, Vol. 15, pp. 307-313.
- [5] J. Shen, B.C. Fabien, "Optimal control of a flywheel energy storage system with a radial flux hybrid magnetic bearing", *Journal of Franklin Institute*, 2002, Vol. 339, pp. 189-210
- [6] Mulcahe, T. M., Hull, J. R., Uherke, K. L. etc. "Flywheel energy storage advanced using HTS bearings", *IEEE Transactions on Applied Superconductivity*, 1999, Vol. 9(2), pp. 297-300.
- [7] O. Tsukamoto, A. Utsunomiya, "HTS flywheel energy storage system with rotor shaft stabilized by feed-back control of armature currents of motor-generator", *Physica C: Superconductivity and its Applications*, 2007, Vol. 463-465, n SUPPL., pp. 1267-1270.
- [8] J. Tzeng, R. Emerson and P. Moy, "Composite flywheel for energy storage", *Composites Science and Technology*, 2006, Vol. 66, pp. 2520-2527.
- [9] X. Dai, Y. Li and H. Yu, "Design of high specific energy density flywheel"(in Chinese), *Journal of Tsinghua University*, 2008, Vol. 48, pp. 379-382.
- [10] M. Ahrens, L. Kuceara, and R. Larsonner, "Performance of a magnetically suspended flywheel energy storage device", *IEEE Transactions on Control system Technology*, 1996, Vol.4, pp. 494-502.
- [11] J.G. Bai, Investigation of active magnetic bearings for flywheel energy storage system. Doctor dissertation (in Chinese), Tsinghua University, Beijing, P.R. China. 2007.