

Comparative analysis methodologies formulation powers in the frequency domain

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Abstract. With the increasing use of non-linear loads in electrical power systems, it is necessary to study the harmonic distortion, which if not considered in the power calculations may result in measurement errors. Therefore, this study aims to present a comparative analysis between two power theories in the frequency domain, Budeanu theory and IEEE 1459 standard, before a case study, in the presence or absence of distortions of a system electrical test.

Key words

Electric power. Harmonic distortion. Imbalance. Quality electricity.

1. Introduction

In order to understand the fact that the power be greater apparent than the consumed active power and to mitigate this, apparent power, without changing the active power delivered to the loads was developed classical theory formulation electrical power in order to better understand and substantiate the transfer of energy in an electrical circuit. However, the whole theory applied to the quantification and power analysis in electrical networks, was implemented by a sinusoidal system, balanced and operating at the fundamental frequency. However, from the 60, Figure 1, there was a significant growth in the use of electronic loads, which have non-linear characteristics, ie, produce whole multiple components and not whole the fundamental, namely: harmonic and interharmonic.

In this context the study of the theory of electric power in the presence of harmonic distortion, shown vital for the analysis and understanding of the energy transfer circuit.

Several research and technical discussions have been developed in order to explain the power of phenomena in non-sinusoidal systems. However, these methods must be compatible and meet the classical theory of powers in sinusoidal regime.

In that order, more precisely in 1927, There was the first theories and formulations developed by Budeanu. Nevertheless, in 1932, Fryze

published his theories and since there is no consensus on the best topology to be applied. Aiming to establish a standard to be adopted by the scientific community and international production, the document of the Institute of Electrical and Electronics Engineers - IEEE 1459 has been established as a basic premise the decomposition of the apparent power in fundamental and not fundamental, demonstrating the power which come from distortions harmonic current and voltage [1], [2].

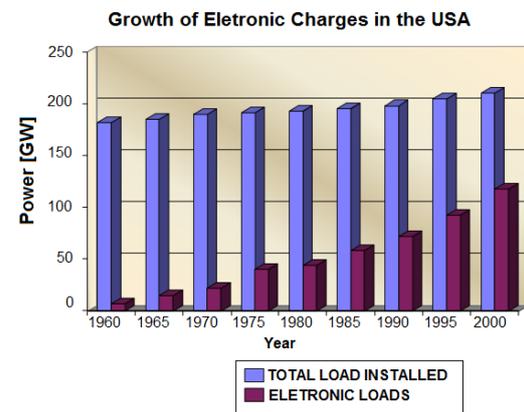


Fig. 1- Growth of electronic loads

Thus, this article presents a comparative analysis of the methodology employed by Budeanu and the IEEE 1459 for the quantification of powers in non-sinusoidal and unbalanced systems, in order to illustrate to the reader the main changes proposed new methodology. For purposes of further discussions, this article is structured as follows: the power of theories, which will be used are presented in section 2. In section 3, it is shown the test system used in this work. In Section 4, the studies are presented by the electrical system employed with the comparisons between the theories of Budeanu and Emanuel (IEEE 1459). In Section 5 the main conclusions are built on the problems studied here.

2. Power formulation methodologies

The main theories of powers under non-sinusoidal conditions, recognized worldwide were proposed in the time domain such as the theories of Czarnecki and Depenbrock, and also in the frequency domain, such as the theories of Budeanu and Emanuel, which is used currently the IEEE. Among these, the theories in the frequency domain will be highlighted, as comparative data between the work, which will be presented are based on proposals Budeanu and Emanuel which have a possibility of expression of power in an electrical system with harmonic distortion.

2.1 Method Budeanu

Constantin Budeanu theory was one of the first and is based on the use of Fourier series defined by Jean B. Fourier to describe the electrical circuit properties such as voltage and current signals. According to Fourier, any signal can be decomposed into a sum as follows:

$$v(t) = V_0 + \sum_{h=1}^{\infty} V'_h \cos(h\omega t) + V_h \sin(h\omega t) \quad (1)$$

Since V_0 the DC component of the signal and the h index of the harmonic order, we have V_h and V'_h how amplitudes of harmonic components and $h\omega$ the angular frequency of each harmonic order. However, since most of the components of an electrical system is represented by odd function and the continuous component being disregarded, V'_h and V_0 becomes equal to zero. So, in instantaneous value has to [3]:

$$v(t) = \sqrt{2} \sum_{m=1}^{\infty} V_m \sin(m\omega t - \varphi_{v_m}) \quad (2)$$

Where V_m is the voltage amplitude and φ_{v_m} the voltage phase angle. The analysis is made for the current analogously. Furthermore, Budeanu postulated that non-sinusoidal conditions, the apparent power can be fractionated into active power and active power does not, the latter being divided into Budeanu reactive power and distortion power which are represented by the following Q_B e D_B , respectively.

$$Q_B = \sum_{h=1}^{\infty} Q_h = \sum_{h=1}^{\infty} V_h I_h \sin \varphi_h \quad (3)$$

$$D_B = \sqrt{\sum_{\substack{n,m \\ n \neq m}}^{\infty} [V_n^2 I_m^2 + V_m^2 I_n^2 - 2V_n I_n V_m I_m \cos(\varphi_m - \varphi_n)]} \quad (4)$$

Therefore, the equation governing the apparent power is given by [1]:

$$S_B = \sqrt{P_B^2 + Q_B^2 + D_B^2} \quad (5)$$

Regarding the power factor represented by Budeanu follows the two equations[2]:

$$fp_B = \frac{P_B}{S_B} \quad (6)$$

$$fp_Q = \frac{P_B}{\sqrt{P_B^2 + Q_B^2}} \quad (7)$$

However, the power formulation defined by Budeanu is very questionable. One major criticism was made by Czarnecki which cites the lack of reactive power input to improve the power factor and the fact that the distortion power has no relation to the distortion of waveforms in a circuit [4]. With this, the update of the IEEE 1459 standard does not mention the concepts of Budeanu.

2.2- IEEE Method 1459

Alexander Emmanuel, president of the group of non-sinusoidal situations studies IEEE proposed a similar power decomposition of the Budeanu which is divided into active power, reactive and distortion. However, this decomposition differs in the way of obtaining the powers, which in this case consists in the separation of the fundamental component of the harmonic components of voltage and current as shown below.

$$V^2 = V_1^2 + \sum_{h=1}^{\infty} V_h^2 = V_1^2 + V_H^2 \quad (9)$$

$$I^2 = I_1^2 + \sum_{h=1}^{\infty} I_h^2 = I_1^2 + I_H^2 \quad (10)$$

Where the index 1 represents the fundamental components and the index h , the harmonics. It is noticed that Alexander makes a square sum of harmonic components of voltage and current, causing the apparent power from (9) and (10):

$$S^2 = V^2 I^2 = (V_1^2 + V_H^2) * (I_1^2 + I_H^2) = (V_1 I_1)^2 + (V_H I_H)^2 + (V_H I_1)^2 + (V_1 I_H)^2 = S_1^2 + D_I^2 + D_V^2 + S_H^2 \quad (11)$$

$$S_H = (V_H I_H) = S_1 \frac{V_H I_H}{V_1 I_1} = S_1 (THD_V)(THD_I) \quad (12)$$

$$P_H = \sum_{h=1} P_h = \sum_{h=1} V_h I_h \cos \theta_h \quad (13)$$

Where S_1 is the apparent fundamental power, D_1 the power of current distortion, D_v the power of voltage distortion, S_H the harmonic apparent power and P_H the harmonic active power which, according to the author, is an indication that reveals the harmonic pollution in charge. It should be remembered that the achievement of the fundamental powers is performed identically to the classic method, it is not necessary here to submit the same. Moreover, the author (Emanuel) relates the fundamental reactive power as needed to improve the power factor. Thus, it defined the apparent no fundamental power S_N that according to Alexander, it would be a good estimate of the size of the harmonic compensator [2].

$$S_N = \sqrt{D_I^2 + D_V^2 + S_H^2} \quad (14)$$

The amount of power related to voltage and current distortion is given by the distortion equations described in (15) and (16).

$$D_V = (V_H I_1) = I_1 \sqrt{\sum_{h=1} V_h^2} \quad (15)$$

$$D_I = (V_1 I_H) = V_1 \sqrt{\sum_{h=1} I_h^2} \quad (16)$$

Similar to performed with voltage, current and power, the power factor also separates the fundamental component, thus it has the real power factor and displacement power factor which are presented respectively by equations (17) and (18).

$$fp = \frac{P}{S} \quad (17)$$

$$fp_1 = \frac{P_1}{S_1} \quad (18)$$

Notably, the calculation of the power factor does not include directly the reactive component, only active power and apparent, unlike Budeanu. Thus, although there is a part that says controversial this formulation, which

refers to the reactive power and distortion on their physical interpretations and definitions for the full power of distortion, this method was adopted by the IEEE Standard 1459 in 2010 and It is used in this work.

3. Computational Modeling: IEEE 1459

For the purpose to evaluate and validate the computational model developed in this article it was used in the electrical system shown in Figure 2. This system refers to a small industrial consumer loads presenting the constant impedance type, constant power and non-linear loads. The electrical arrangement resembles a real power system and, second, the author, this is represented by a three-phase voltage source in series with an equivalent impedance which represents the short circuit system level.

It has been dealing with consumer unit, this contains linear loads and a bank of capacitors for power factor correction. Moreover, to represent non-linear loads, there are sources of harmonic current. To develop the model, figure 2, we used the software ATPDraw, thus the data required for the implementation thereof were taken from reference [5].

In order to carry out a comparative analysis between the Budeanu methodology and the proposed IEEE 1459, a computer interface was developed in Matlab software, using as a resource to guide tool, oriented language software object. In this regard, considering the equations (9) to (18) as well as all formulations used the classic method of power calculation for key components held code development and its subsequent validation using as parameter reference [2]. After this stage, it was initiated the development of the graphical interface shown in Figure 3.

By observing the interface, it can see that the user must enter the data voltage, current and their proper angles in order to obtain the values expressed by the letters corresponding to the rule mentioned in the previous section, IEEE 1459. For the power calculations, who regard voltage amplitudes or current of each harmonic order, it was considered to the 25th harmonic order, to meet the module 8 of the Distribution Procedures - PRODIST, [6]. It is noteworthy that the data to be obtained are single-phase, so phase-neutral.

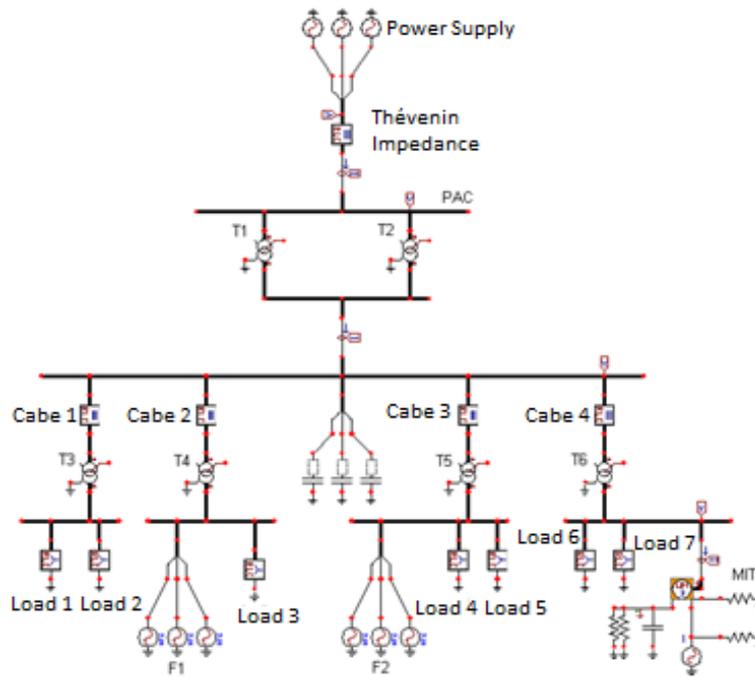


Fig.2- Electrical Test System.

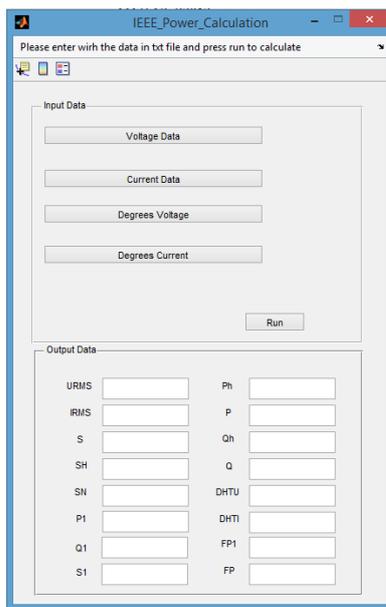


Fig. 3 Graphical Interface for Power Calculation.

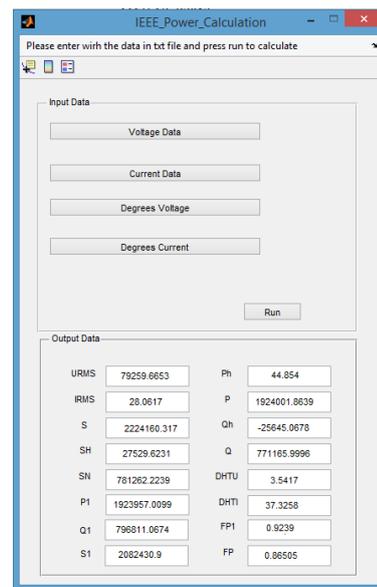


Fig.4-values obtained by Case II data.

In order to validate the developed program, we used the test system shown previously, Figure 2, and the data indicated in Table 5 in the next section, case studies. Thus, the values shown in the figure was obtained 4. The values in the interface were compared to the values submitted by reference [2], which the author was used the same case study and the same equations presented for power calculation . Thus, the implementation of the code along with the graphical interface, in a way, accelerates the calculation power because this interface has been developed in order to obtain practical results, efficient and teaching.

4. Case Study

In this section the case studies will be presented with different operating conditions for electrical testing system. The analyzes for this study will be carried out with emphasis on the point of common coupling between a system supplier and an industrial consumer unit. The studies were oriented along the reference [2] for comparison purposes. After the presentation of this, the power will be applied methodologies described in section 2 with a critical analysis for each case.

4.1 Case I

In this case, the supply voltage is purely sinusoidal and there are no nonlinear loads, i.e. without sources of current and voltage harmonics, but the presence saturation of the ferromagnetic core of the transformer generates small harmonic distortion current. Analyzing only phase A for all the cases, Table 1 shows the effective values of voltage, current and individual harmonic distortion of voltage and current which are calculated based on equations (19) and (20) respectively.

$$DIT_h \% = \frac{V_h}{V_1} \cdot 100 \quad (19)$$

$$DII_h \% = \frac{I_h}{I_1} \cdot 100 \quad (20)$$

Table 1- Operating Conditions I

Harmonic Ordem	Neutral-Phase Voltage		Current	
	[V]	DIT [%]	[A]	DII [%]
1 ^a	79210 ∠ -1,017°	-	26,27 ∠ -23,5°	-
5 ^a	54,54 ∠ 179,5°	0,07	0,0564 ∠ 113,1°	0,21
7 ^a	43,8 ∠ -79,1°	0,06	0,0174 ∠ 164°	0,07
11 ^a	20,15 ∠ -167,8°	0,03	0,0207 ∠ 86,94°	0,08
13 ^a	19,47 ∠ -170,6°	0,02	0,0096 ∠ 97,79°	0,04

It should be noted that although the table is present only 5 components, all calculations are made to the 25th harmonic order.

In Table 2, the application of the first case is presented in all the equations (2) to (7), mentioned in section 2 as Budeanu method, with values of single-phase power. In Table 3, application in all the equations (9) is displayed (18) as Emanuel method.

Table 2- Budeanu method for Case I

S_B	P_B	Q_B	D_B	fp_B	fp_Q
2080.88kVA	1922.711 kW	795.741 kVAr	6.28 kVA	0.924	0.924

Noting the above tables, it can see the proximity of the values of power and power factor. Thus, it appears the validity and similarity of two theories for sinusoidal systems. Note also that the harmonic current distortion rate is much higher compared to voltage. Regarding the power Budeanu distortion, this has a high value, thus showing a lack of physical interpretation of it.

Table 3- Emanuel Method for Case I

S		P		P_H	
2080.88 kVA		1922.711 kW		0.023 kW	
S_1		P_1		Q_1	
2080.8466 kVA		1932.688 kW		795.735 kVAr	
S_N	TDH_I	TDH_U	S_H	fp	fp_1
11.759 kVA	0.44%	0.36%	0.032 kVA	0,924	0,924

4.2 Case II

In this case, inserted into non-linear loads in the system, i.e., current sources which have effective values according to Table 4 [5] and the data obtained are shown in Table 5 [2].

Table 4- Current Sources

Current Source	5 ^o Ordem Harmonics of the Current [A]	7 ^o Ordem Harmonics of the Current [A]	11 ^o Ordem Harmonics of the Current [A]	13 ^o Ordem Harmonics of the Current [A]
F1	1446,03 ∠ -12,35°	963,36 ∠ -123,15°	410,69 ∠ 118,10°	404,25 ∠ -50,40°
F2	1035,49 ∠ -0,60°	857,72 ∠ -109,81°	382,69 ∠ 152,79°	362,32 ∠ -29,50°

Table 5- Operating Conditions II

Harmonic Ordem	Neutral-Phase Voltage		Current	
	[V]	DIT [%]	[A]	DII [%]
1 ^a	79210 ∠ -1,023°	-	26,29 ∠ -23,52°	-
5 ^a	1378 ∠ 133°	1,74	7,071 ∠ -139,3°	26,90
7 ^a	1436 ∠ -100°	1,81	5,326 ∠ -8,331°	20,26
11 ^a	1136 ∠ -87,68°	1,43	2,693 ∠ 3,781°	10,24
13 ^a	1593 ∠ -23,62°	2,01	3,528 ∠ 67,12°	12,39

Thus, in Tables 6 and 7 shows the results for the Budeanu and Emanuel methods.

Table 6- Budeanu method for Case II

S_B	P_B	Q_B	D_B	fp_B	fp_Q
2224.16 kVA	1924.002 kW	771.166 kVAr	806,479 kVA	0.865	0.928

Table 7- Emanuel method for Case II

S		P		P_H	
2224.16 kVA		1924.002 kW		0.045 kW	
S_1		P_1		Q_1	
2082.431 kVA		1923.957 kW		796.811 kVAr	
S_N	TDH_I	TDH_U	S_H	fp	fp_1
781.263 kVA	3.54%	37.33%	27,5297 kVA	0,865	0,924

Observing the reactive power data Budeanu, disability just to perceive when compared to the fundamental. It is noticed that this value is smaller, making it clear that there are negative harmonic reactive power. Moreover, Budeanu deficiency is perceived according to the calculation of the power factor fp_B , and uses the power of distortion fp_Q and discards. By comparing the harmonic distortion of both voltage and current, it is clear that these values are much higher in the second case.

4.3 Case III

In this case, the supplement is unbalanced with values shown in Table 8 and the consumer has only linear loads. The data obtained from the system are presented in Table 9.

Table 8- Unbalance Power Supply

Power Supply	Phase-Phase Voltage (kV)
Fase A	140,76 ∠ 0°
Fase B	136,641 ∠ -121,002°
Fase C	136,641 ∠ 121,002°

Table 9- Operating Conditions III

Harmonic Ordem	Neutral-Phase Voltage		Current	
	[V]	DIT [%]	[A]	DII [%]
1 ^a	80800 ∠ -1,011°	-	26,86 ∠ -23,67°	-
5 ^a	56 ∠ 179,3°	0,07	0,0548 ∠ 114,7°	0,20
7 ^a	44,92 ∠ 179°	0,06	0,0177 ∠ 169,3°	0,07
11 ^a	20,36 ∠ -167°	0,02	0,0224 ∠ 84,01°	0,08
13 ^a	19,51 ∠ -169,4°	0,02	0,0106 ∠ 92,51°	0,04

Thus, the tables 10 and 11 are presented the results for the Budeanu and Emanuel methods for this case.

Table 10- Budeanu method for Case III

S_B	P_B	Q_B	D_B	fp_B	fp_0
2088.126 kVA	1930.069 kW	796.886 kVAr	8.835 kVA	0.924	0.924

Table 11- Emanuel method for Case III

S		P		P_H	
2088.126 kVA		1930.069 kW		0.014 kW	
S_1		P_1		Q_1	
2088,103 kVA		1930.055 kW		796.884 kVAr	
S_N	TDH_I	TDH_U	S_H	fp	fp_1
9.739 kVA	0.44%	0.36%	0.022 kVA	0,924	0,924

In the case of voltage unbalance, it can see changes in the values of power, but it did not alter the power factor when compared to the first case, since the load conditions were maintained and the analysis is done similarly to the case I.

4.4 Case IV

In this case, the balance is maintained and the consumer presents linear and nonlinear loads. The data obtained are shown in Table 12.

Table 12- Operational Condition IV

Harmonic Ordem	Neutral-Phase Voltage		Current	
	[V]	DIT [%]	[A]	DII [%]
1ª	80790 ∠ -1,023°	-	26,86 ∠ -23,71°	-
5ª	1377 ∠ 133,1°	1,70	7,061 ∠ -139,3°	26,29
7ª	1436 ∠ -99,97°	1,78	5,322 ∠ -8,226°	19,81
11ª	1133 ∠ -87,78°	1,40	2,683 ∠ 3,714°	9,99
13ª	1587 ∠ -23,71°	1,96	3,247 ∠ 67,05°	12,09

Thus, Tables 13 and 14 show the results for the methods already discussed. For non-sinusoidal regimes as presented in the case IV, where there is so much imbalance and harmonic current sources, the difference between conventional methods and studied in this work is even more worse. Comparing this case with Case II, it is observed that the value of the harmonic distortion have more interference than the voltage imbalance. Moreover, when changing the system power, the harmonic active power has been increased due to the influence of this change in circuit components. We notice also that the distortion values are higher when compared to the case III, since it entered non-linear loads.

Table 13- Budeanu method for Case IV

S_B	P_B	Q_B	D_B	fp_B	fp_0
2228.862 kVA	1927.734 kW	772.145 kVAr	809.604 kVA	0.865	0.928

Table 14- Emanuel method for Case IV

S		P		P_H	
2228.862 kVA		1927.734 kW		0.123 kW	
S_1		P_1		Q_1	
2086.184 kVA		1927.611 kW		797.769 kVAr	
S_N	TDH_I	TDH_U	S_H	fp	fp_1
784.527 kVA	3.47%	36.48%	27.529 kVA	0,865	0,924

5. Conclusion

Thus, through the analyzes presented here, it is clear the need to define a method for non-sinusoidal situations, since the classical method of power calculation does not account for the influence of harmonic distortion and voltage imbalance, which may be a factor harmful when it comes to power measurement in an electrical system whose distortions are present. Therefore, this work presents a comparative study between two power theories of Budeanu and IEEE 1459 standard, used on a large scale today. However, it is evident this article disability of the first method with respect to reactive power distortion, which is, in the case of harmonic distortion, less than the fundamental reactive power, that is, there are big differences in reactive power calculations and distortion to the methods. However, referring to the values of active power is no similarity between the two methods. Furthermore, with regard to the imbalance it can be noted that both cases is not of a specific calculation for this. Thus, it is noted that there are flaws in all methods and then the choice of the appropriate method depends on the implementation.

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